

# TSTE25 Power Electronics

Lecture 2  
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ISY/FS

# Outline

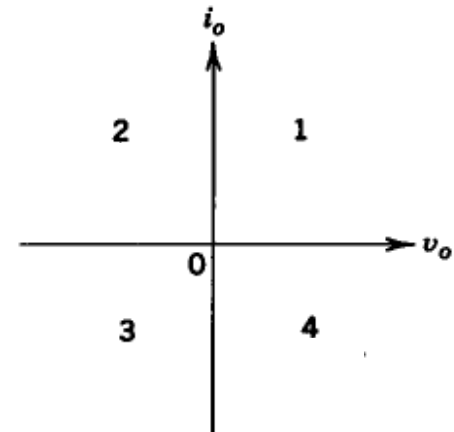
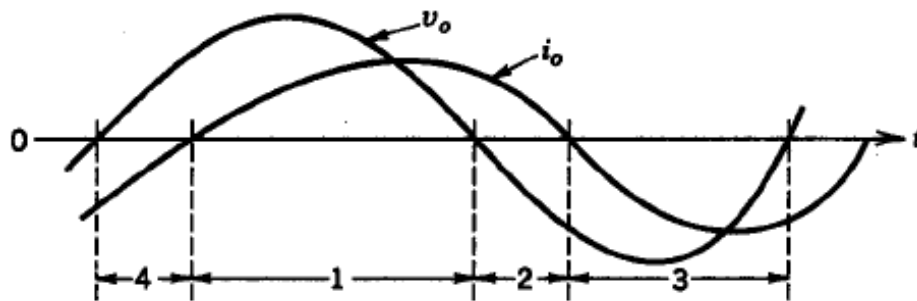
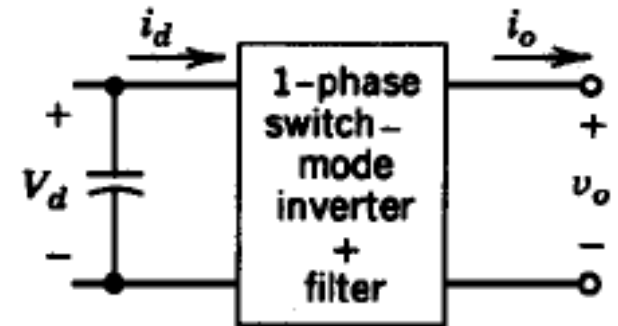
- DC-AC switching inverters
  - Switch-mode principle
  - Single-phase inverter
    - Half-bridge
    - Full-bridge
  - PWM switching
  - Full-bridge DC/DC converter

# Switch-mode dc-ac inverter

- Sinusoidal ac
- Controlled magnitude
- Controlled frequency
- Common use
  - Ac motor drive
  - Uninterruptable ac power supply
  - 12V DC -> 230V AC inverter

# Switch-Mode DC-AC Inverter

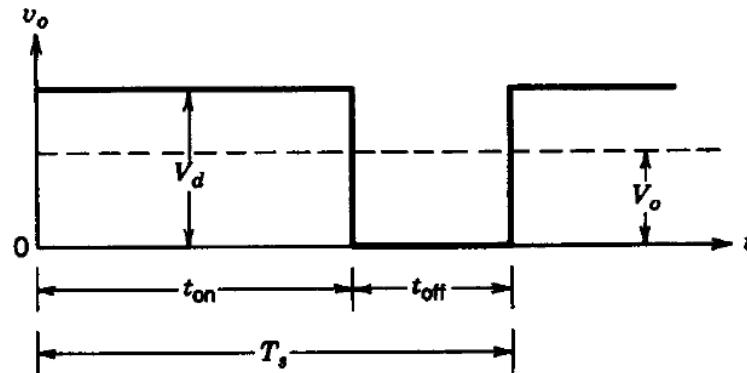
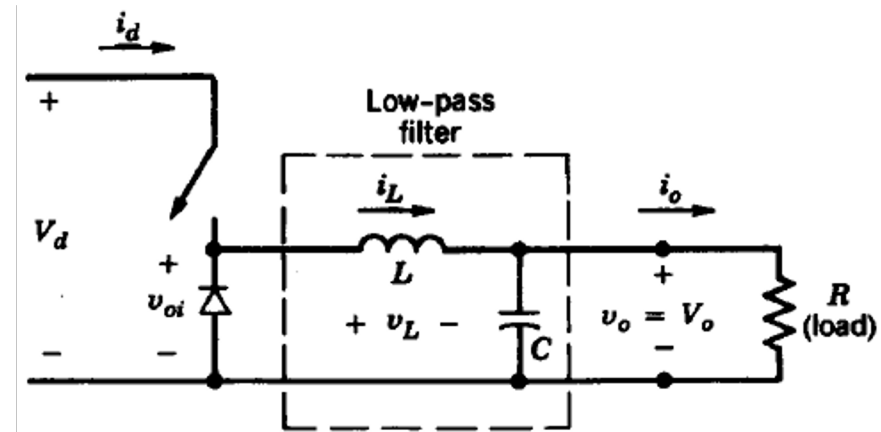
- Fixed dc-voltage
- Switched output filtered to generate sinusoidal  $v_o$
- Assume inductive load at  $v_o$ ,  $i_o$  lagging
- Waveforms in all four quadrants



# Compare: Step-down (buck) converter

- Output voltage amplitude controlled by switch duty cycle

$$\frac{V_o}{V_d} = D$$



# Compare: Step-up (boost) converter

- Voltage ratio defined by duty cycle

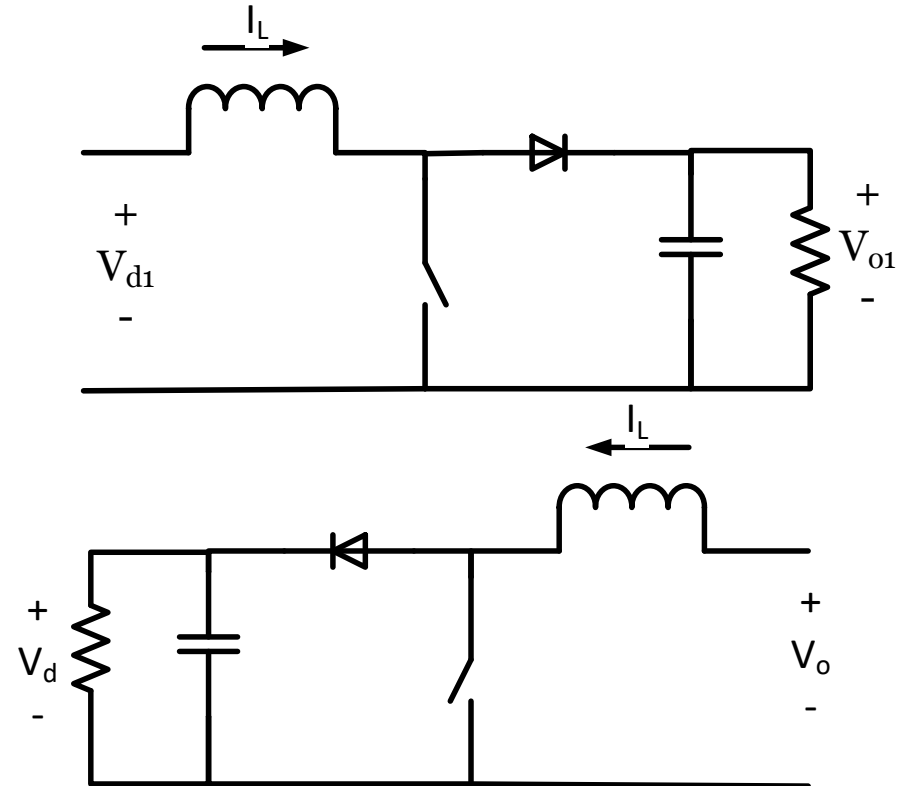
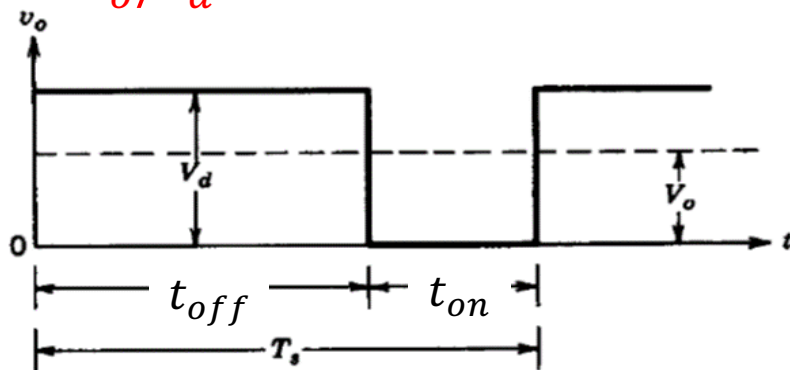
$$V_{o1}/V_{d1} = \frac{1}{1 - D}$$

- Current from low voltage side to high voltage side

- **Inverted Boost converter**

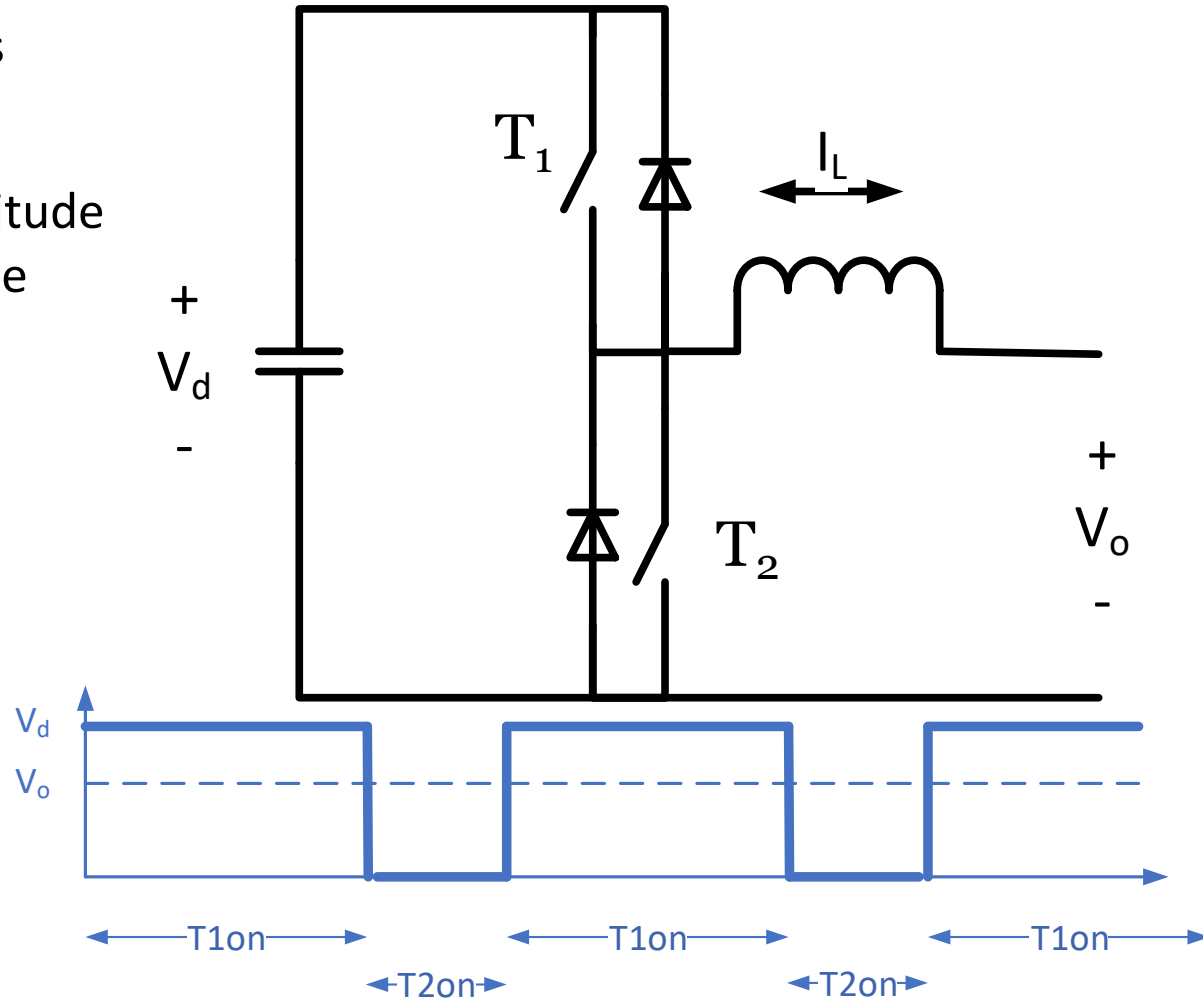
$$V_o = V_{d1}, V_d = V_{o1}$$

$$V_o/V_d = 1 - D$$



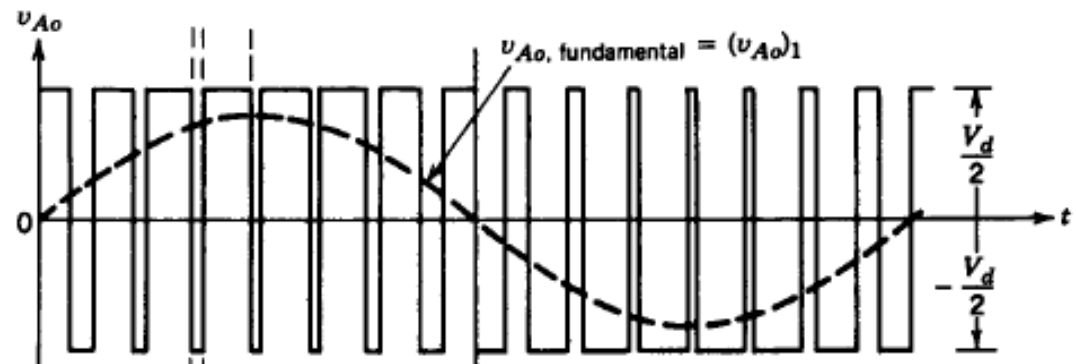
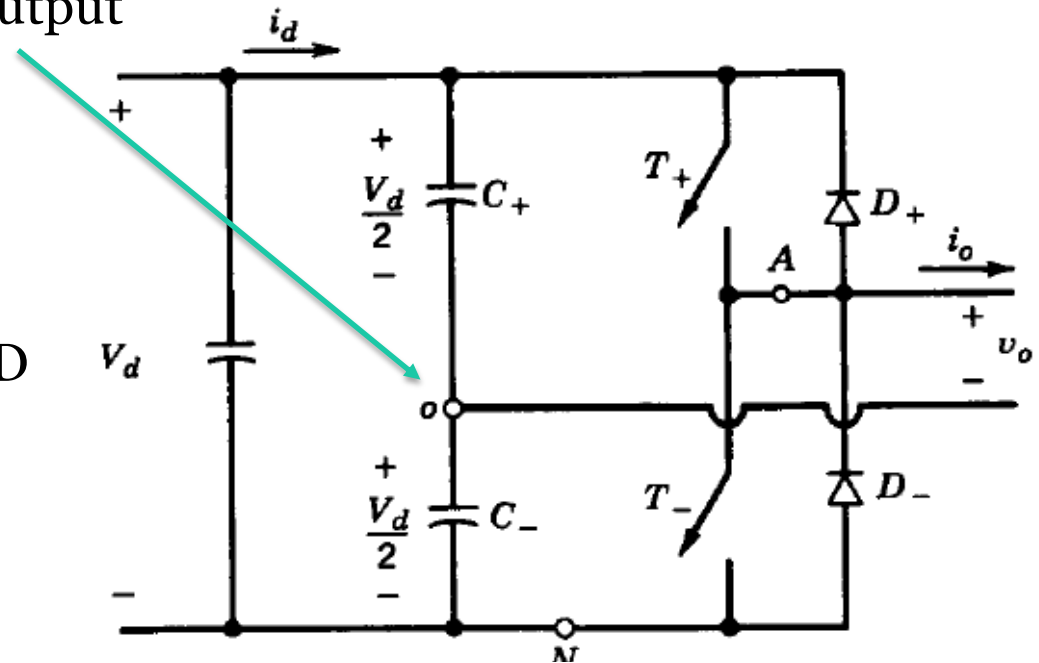
# Half-bridge(2-level) DC/DC converter

- 2 output voltage levels
  - $(V_d, 0)$
- Average voltage magnitude controlled by duty cycle
  - $V_o/V_d = D(T_1)$
  - $D(T_2) = 1 - D(T_1)$
- Bi-directional current
- Forbidden state:
  - $T_1$  and  $T_2$  both on
  - Short **circuit**



# Half-bridge (2-level) DC/AC converter

- DC-side midpoint 'o' reference point for ac-output
- Output voltage,  $v_{Ao}$ , switched between  $+\frac{V_d}{2}$  and  $-\frac{V_d}{2}$
- Sinusoidal variation of D
  - Ac output voltage

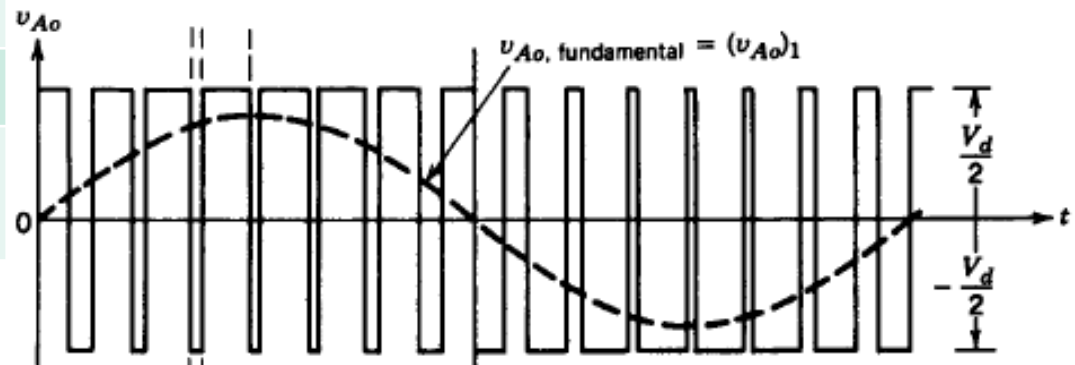
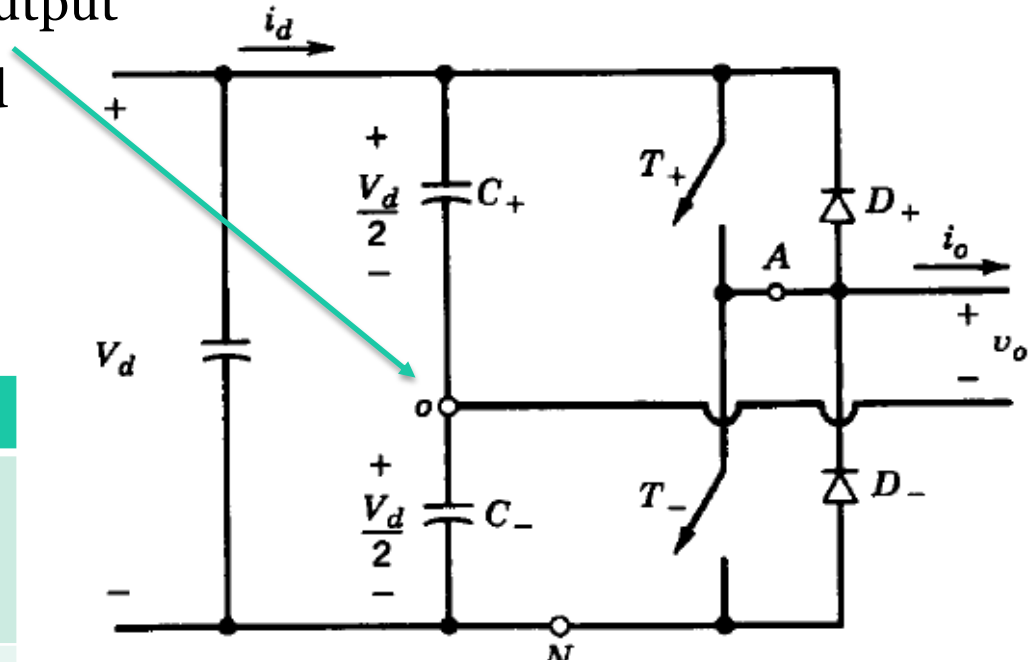




# Half-bridge (2-level) converter

- DC-side midpoint 'o' reference point for ac-output
- Output voltage switched between  $+\frac{V_d}{2}$  and  $-\frac{V_d}{2}$
- 4 possible switch states:

T+	T-	
Off	Off	$v_o-o$ def by $i_o$ . $i_o > 0: v_o-o = -V_d/2$ $i_o < 0: v_o-o = +V_d/2$
On	Off	$v_o-o = +V_d/2$
Off	On	$v_o-o = -V_d/2$
On	On	Short circuit. Forbidden state





# DC/AC-converter control

- Pulse width modulation, PWM, to control switching
- Switching frequency,  $f_s$ , the repetition rate of turn-on/off

–  $v_{tri}$ , triangular signal between -1 and +1

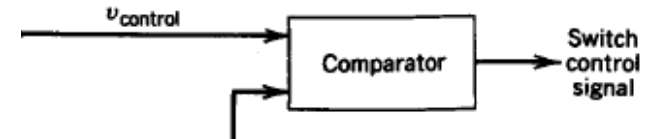
- Reference signal,

$$v_{control} = m_a \sin \omega_1 t$$

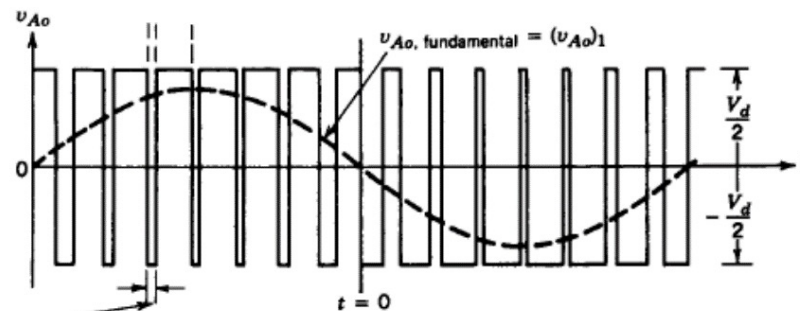
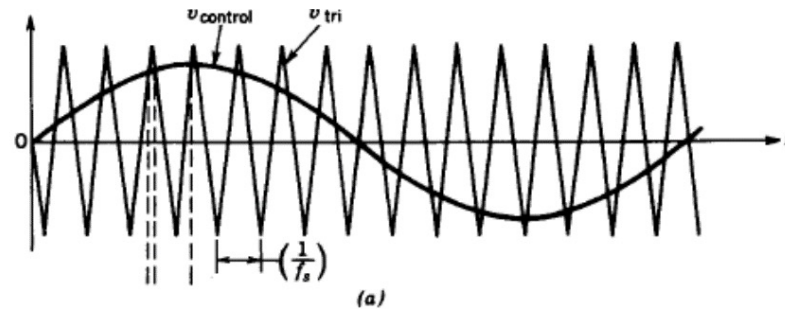
–  $0 < m_a < 1$

- Output voltage:

$$V_{A0} = m_a \frac{V_d}{2} \sin \omega_1 t$$



(a) Tri-angular signal,  $v_{tri}$

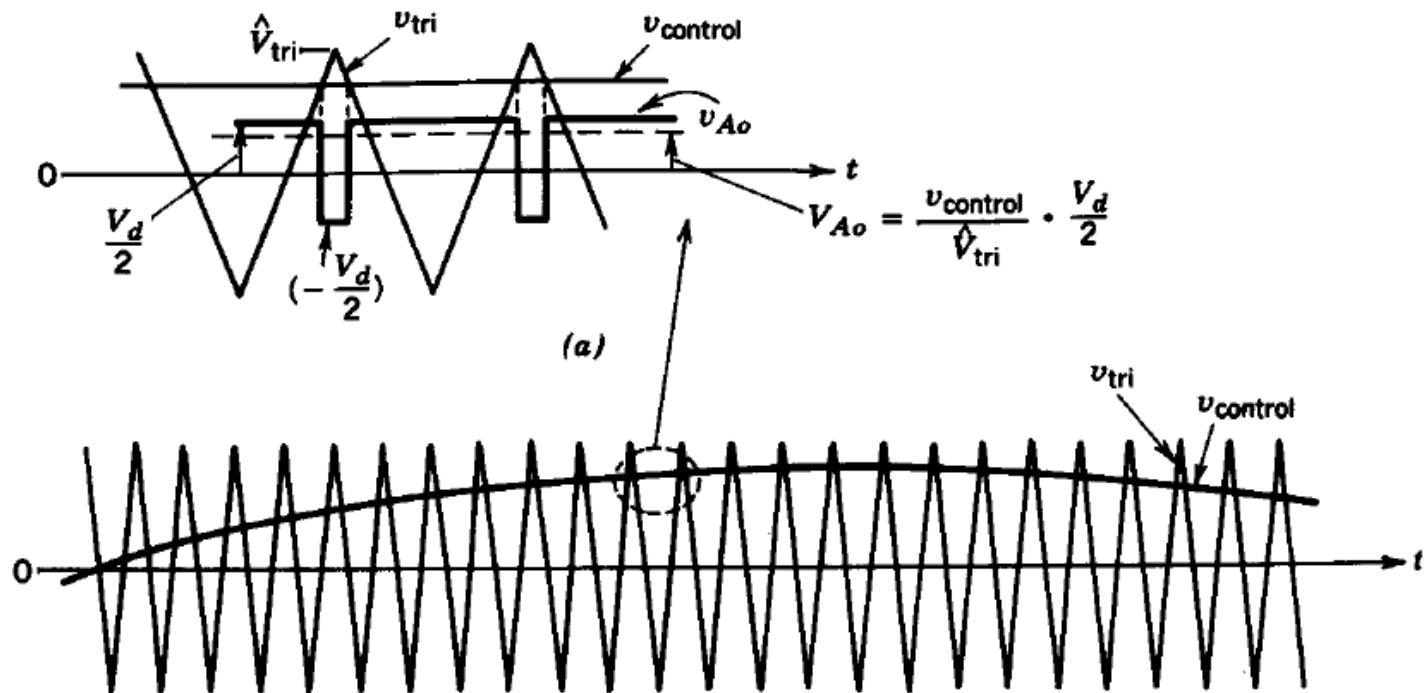


$\left\{ \begin{array}{l} v_{control} < v_{tri} \\ T_{A-}: \text{ on, } T_{A+}: \text{ off} \end{array} \right\}$ 
 $\left\{ \begin{array}{l} v_{control} > v_{tri} \\ T_{A+}: \text{ on, } T_{A-}: \text{ off} \end{array} \right\}$

# PWM modulation control

- Fundamental frequency output,  $\hat{V}_{ao1} \sin \omega_1 t$
- $0 < m_a < 1$ , linear range

$$\hat{V}_{ao1} = m_a \frac{V_d}{2}$$



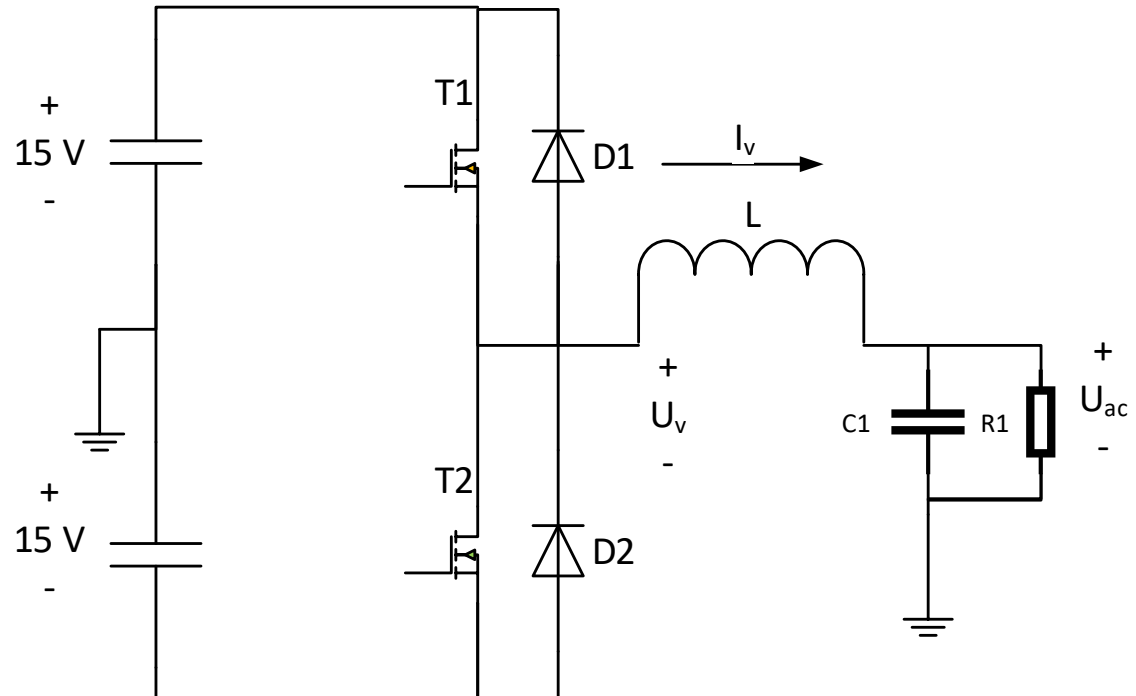
# Half-bridge converter example

- Total dc-voltage, positive-to-negative side

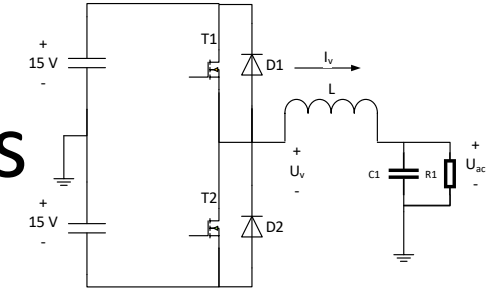
$$- U_d = 30V$$

- DC-voltage positive and negative side to ground

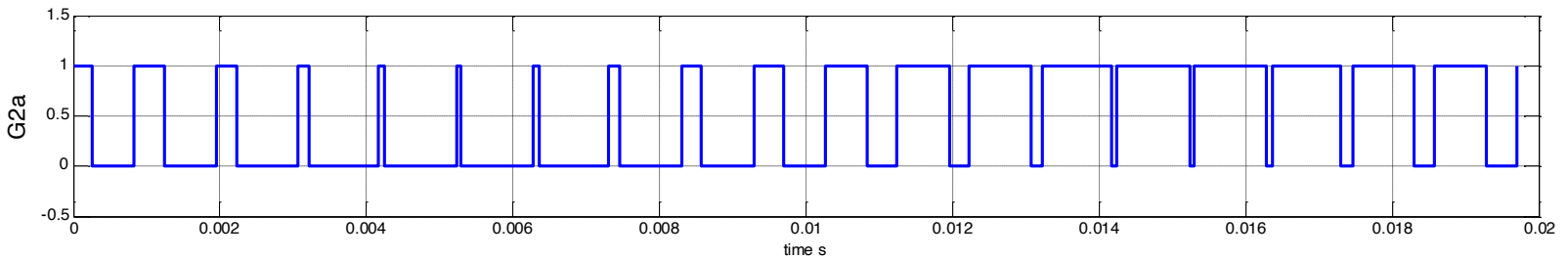
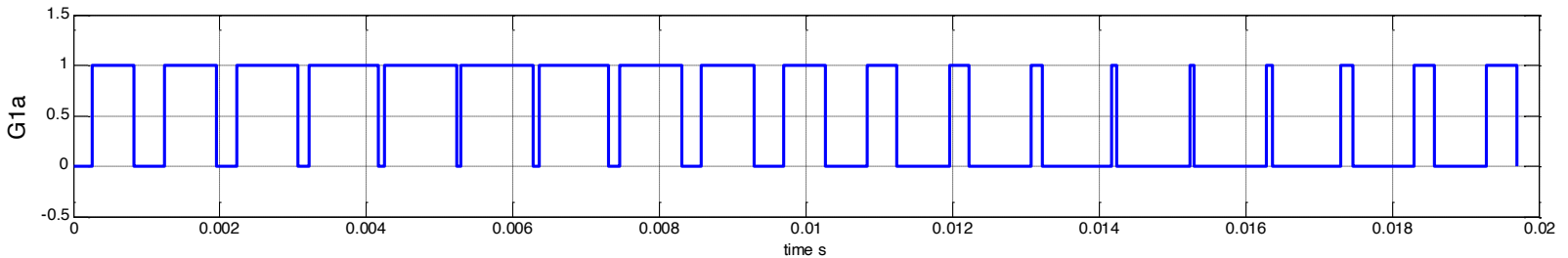
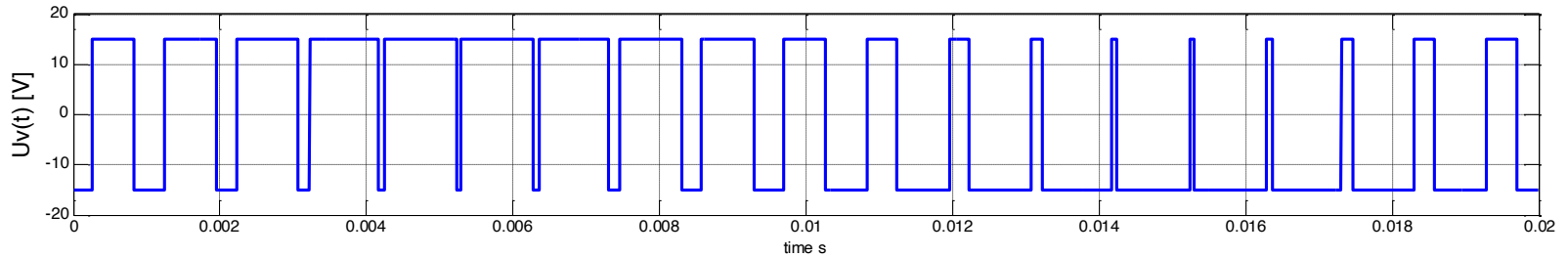
$$- \frac{U_d}{2} = \pm 15V$$



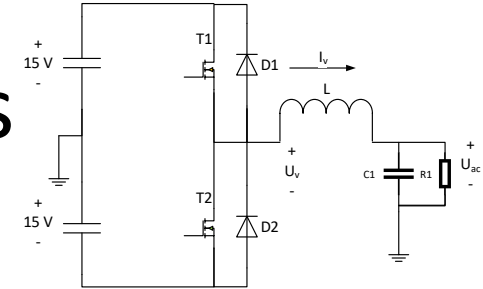
# Output voltage & gate signals



TSTE19 2-level inverter

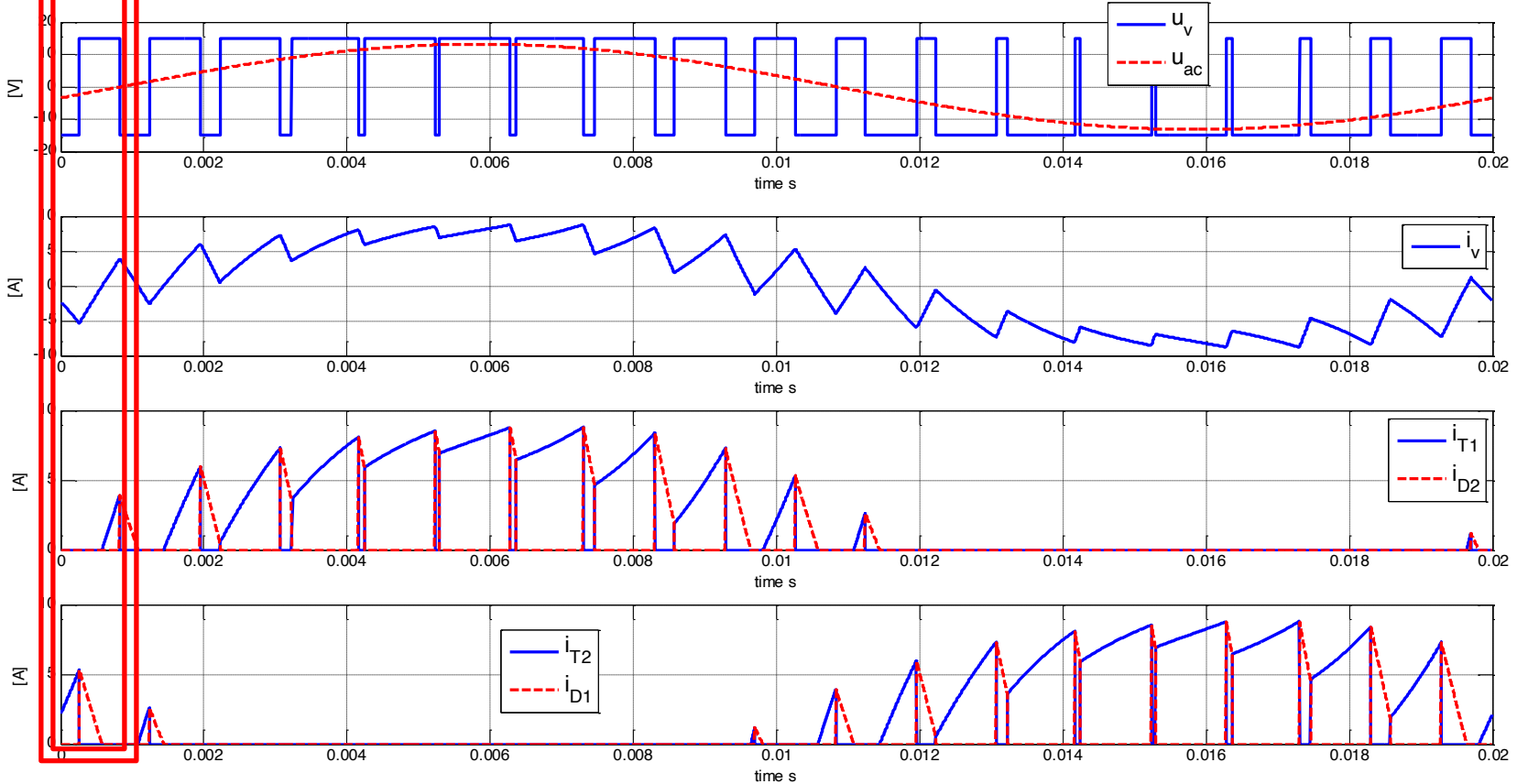


# Voltage & current waveforms



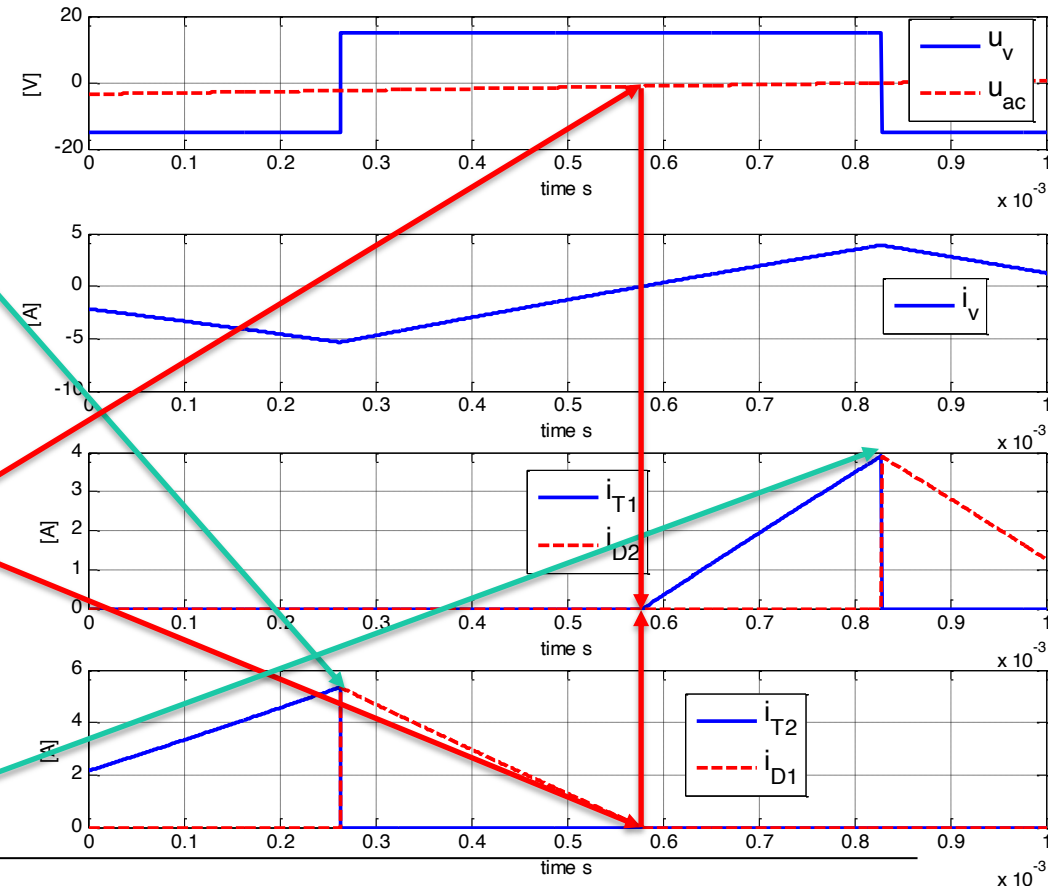
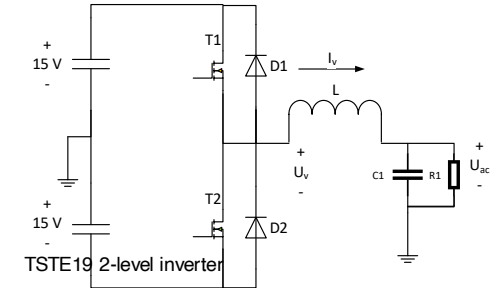
Zoom in 1st ms.

TSTE19 2-level inverter



# Zoom in of 1st ms

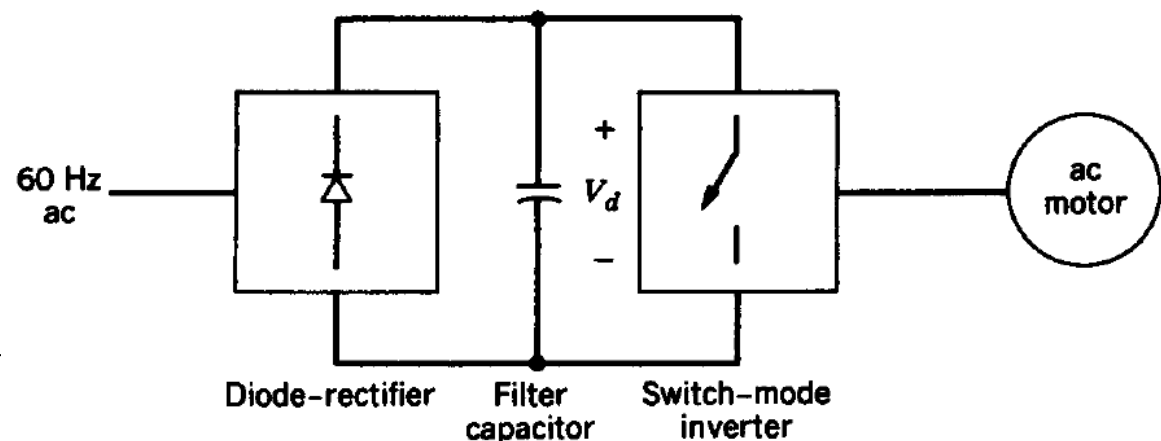
- $t < 0.27$  ms,
  - T2 on
  - $i_v < 0$
- $t = 0.27$  ms,
  - G2 off, G1 on
  - $i_v < 0$
  - T2 to D1 commutation
- $t = 0.57$  ms,
  - $i_v > 0$
  - D1 to T1 conducting
- $t = 0.83$  ms,
  - G1 off, G2 on
  - T1 to D2 commutation





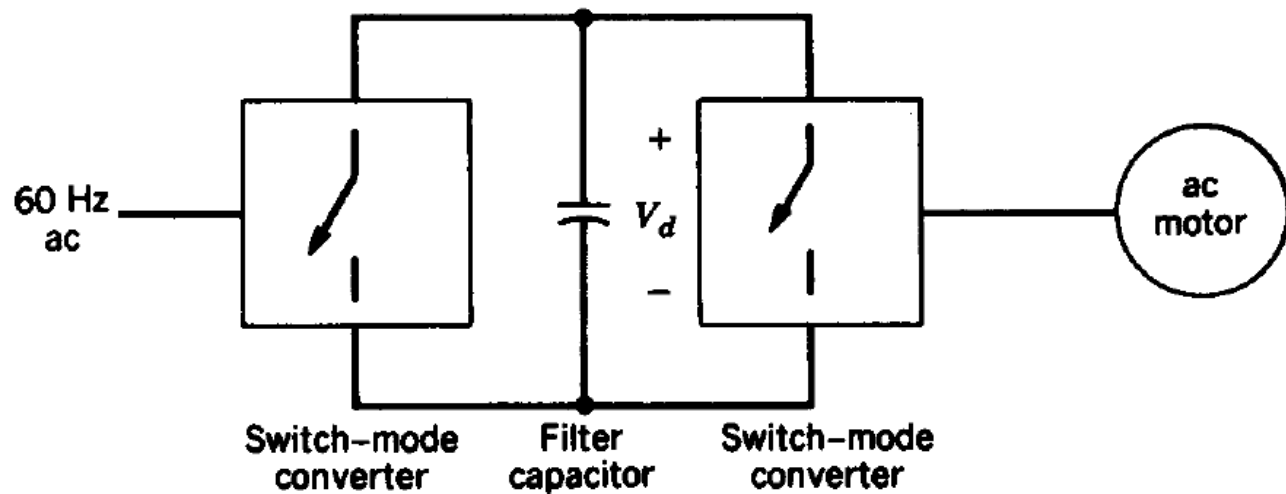
# Unidirectional AC-AC converter

- Switch-mode inverter allow power reversal back to DC
- Motor sometimes behaving as a generator
- Use large filter capacitor to temporary store energy from ac motor
- May sometimes add resistor on DC to dissipate energy from motor braking



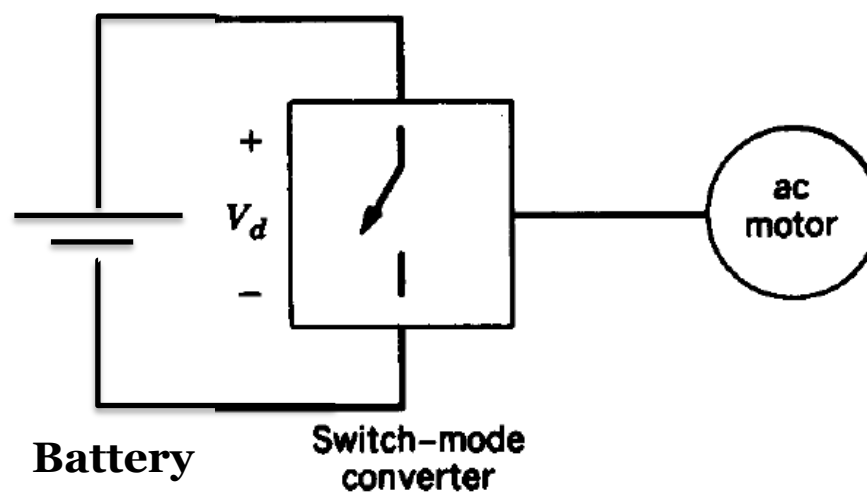
# Bidirectional AC-AC converter

- When DC node can not accept all braking power from ac-motor backfeed into ac-grid is used
- E.g. train braking, HVDC



# Bidirectional AC-motor drive

- Battery supplied motor drive
- Regenerative braking gives battery charging



# Lecture 3

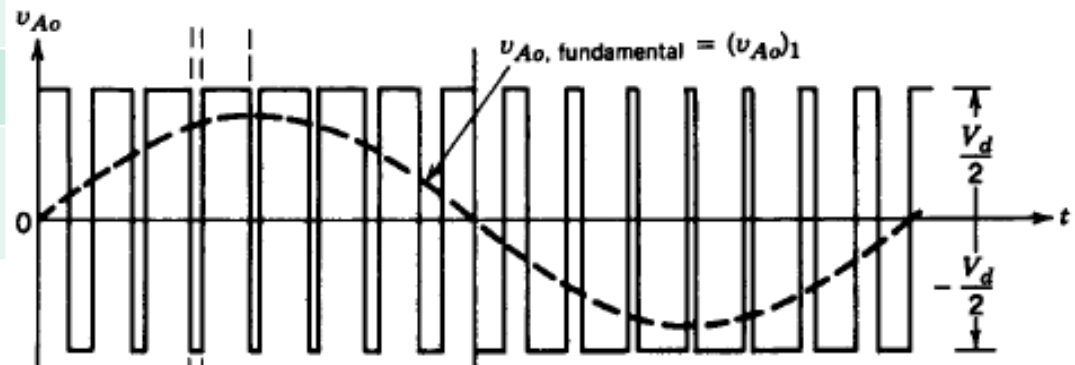
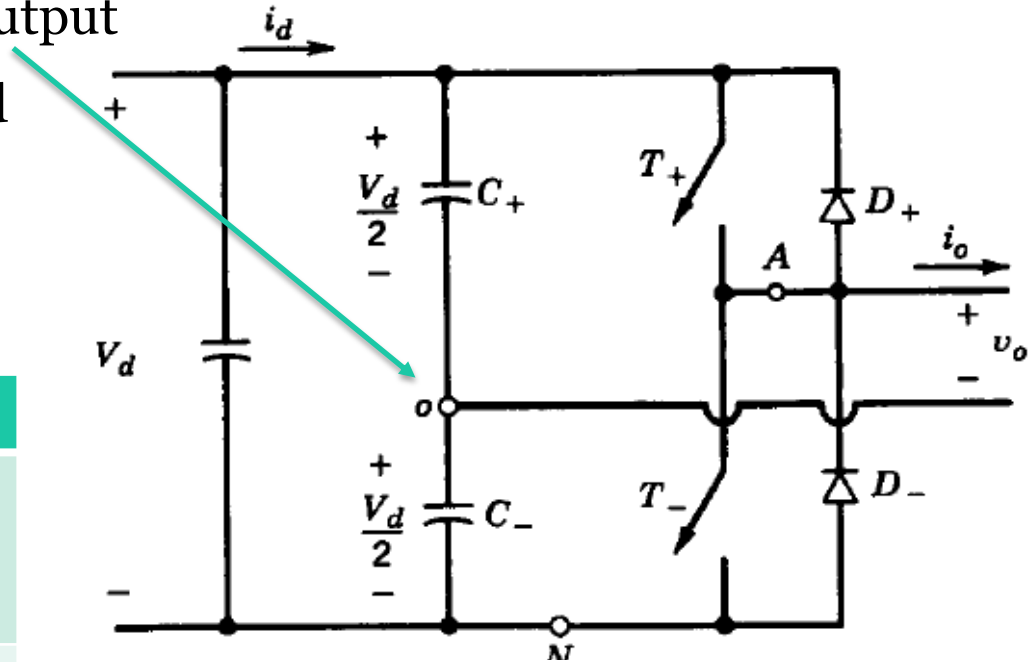
## Full-bridge inverter

# Half-bridge (2-level) converter

$$\hat{V}_{Ao1} = m_a \frac{V_d}{2}$$

- DC-side midpoint 'o' reference point for ac-output
- Output voltage switched between  $+\frac{V_d}{2}$  and  $-\frac{V_d}{2}$
- 4 possible switch states:

T+	T-	
Off	Off	$v_o-o$ def by $i_o$ . $i_o > 0: v_o-o = -V_d/2$ $i_o < 0: v_o-o = +V_d/2$
On	Off	$v_o-o = +V_d/2$
Off	On	$v_o-o = -V_d/2$
On	On	Short circuit. Forbidden state

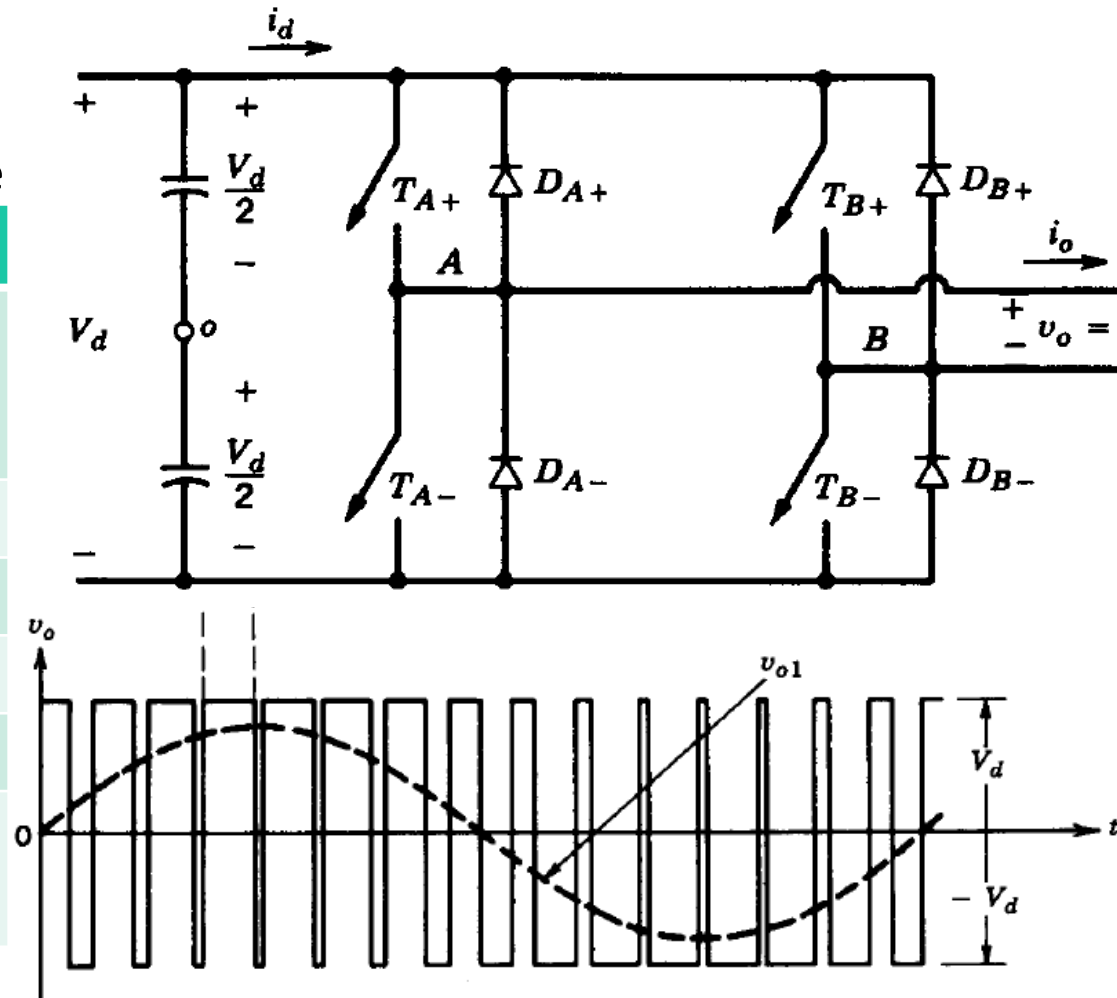


# Full-bridge inverter

- Maximum output voltage doubled compared to half-bridge inverter
- No need for midpoint voltage

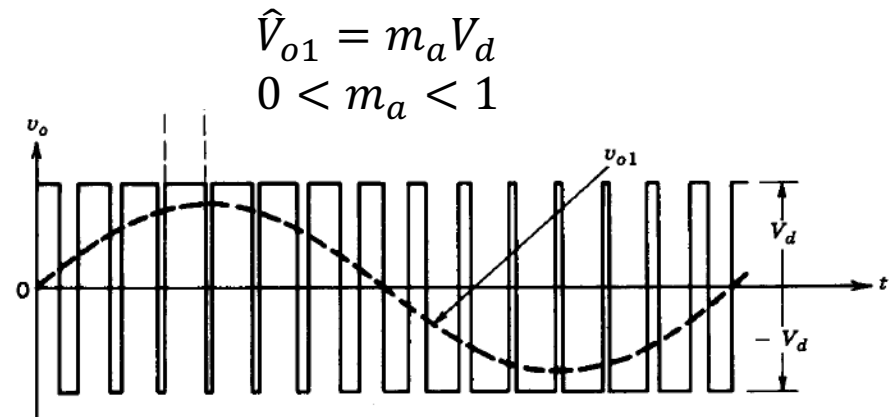
$$\hat{V}_{o1} = m_a V_d$$

$T_{A+}$	$T_{A-}$	$T_{B+}$	$T_{B-}$	
Off	Off	Off	Off	Output isolated. Unless $v_o > V_d$ by external source
On	Off	On	Off	$v_o = 0$
On	Off	Off	On	$v_o = +V_d$
Off	On	On	Off	$v_o = -V_d$
Off	On	Off	On	$v_o = 0$
On	On	x	x	Short circuit, Forbidden states
x	x	On	On	Forbidden states

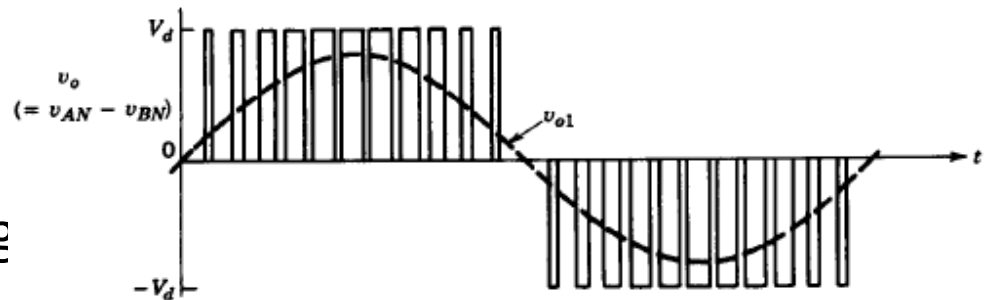


# PWM switching strategies

- Bipolar voltage switching
  - Only two states used for (TA+, TA-, TB+, TB-) giving output voltage:  $+V_d$  or  $-V_d$

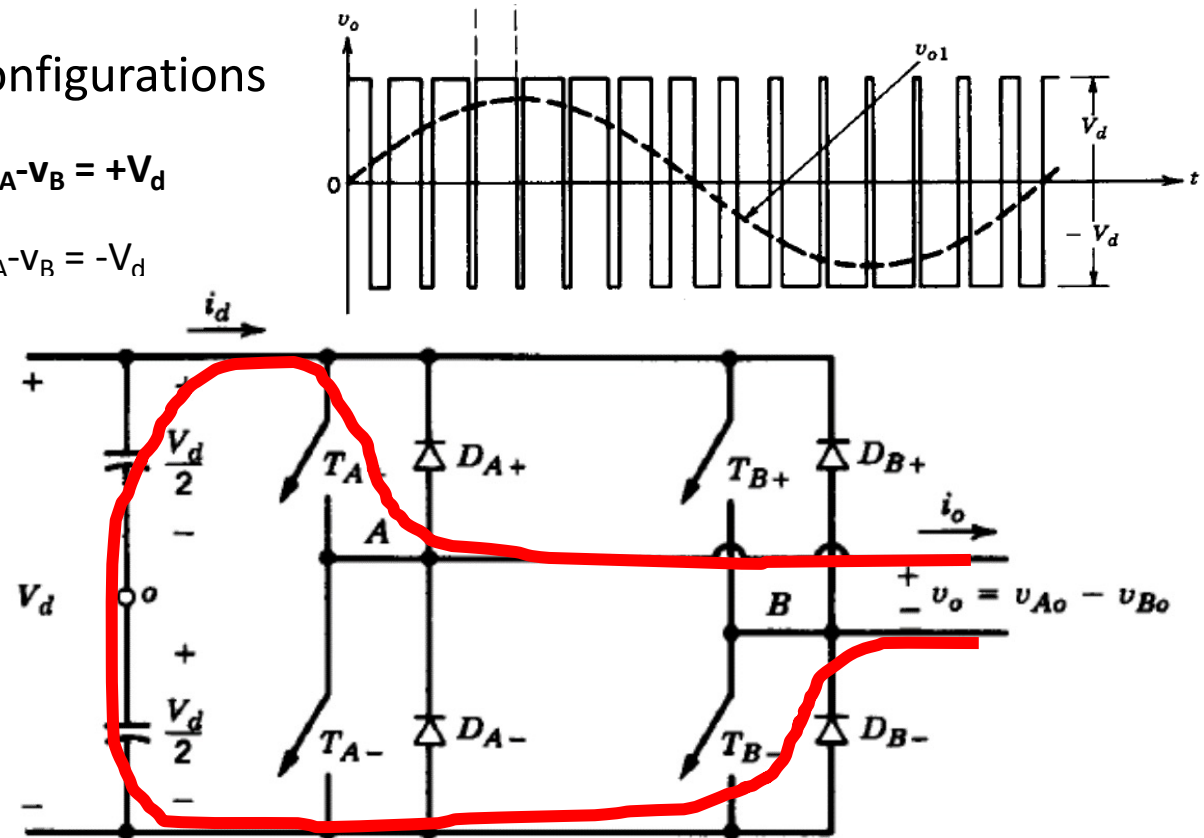


- Unipolar switching
  - All four states used (TA+, TA-, TB+, TB-) giving output voltage  $+V_d$ , 0 or  $-V_d$



# PWM bipolar switching

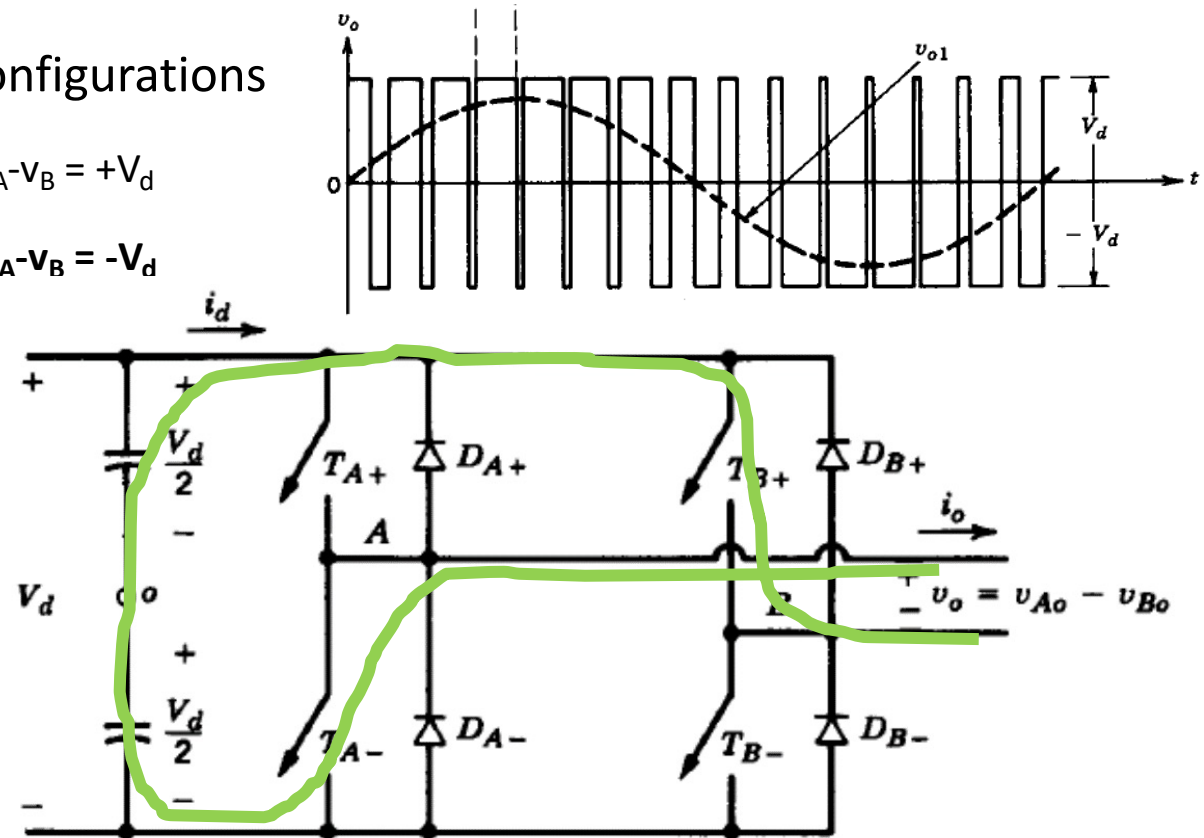
- Bipolar voltage switching
  - Both pairs ( $T_{A+}$ ,  $T_{B-}$ ) and ( $T_{A-}$ ,  $T_{B+}$ ) controlled simultaneous
- 2 possible switch configurations
  1.  $T_{A+}$  on,  $T_{B-}$  on:  $v_o = v_A - v_B = +V_d$
  2.  $T_{A-}$  on,  $T_{B+}$  on:  $v_o = v_A - v_B = -V_d$





# PWM bipolar switching

- Bipolar voltage switching
  - Both pairs ( $T_{A+}$ ,  $T_{B-}$ ) and ( $T_{A-}$ ,  $T_{B+}$ ) controlled simultaneous
- 2 possible switch configurations
  1.  $T_{A+}$  on,  $T_{B-}$  on:  $v_o = v_A - v_B = +V_d$
  2.  $T_{A-}$  on,  $T_{B+}$  on:  $v_o = v_A - v_B = -V_d$



# PWM bipolar switching

- Both legs switch at the same time defined by  $v_{\text{control}}$  and  $V_{\text{tri}}$
- When  $T_{A+}$  switches on  $T_{B+}$  switches off
- Output voltage
  - $\hat{V}_{o1} = m_a V_d$
  - $0 < m_a < 1$

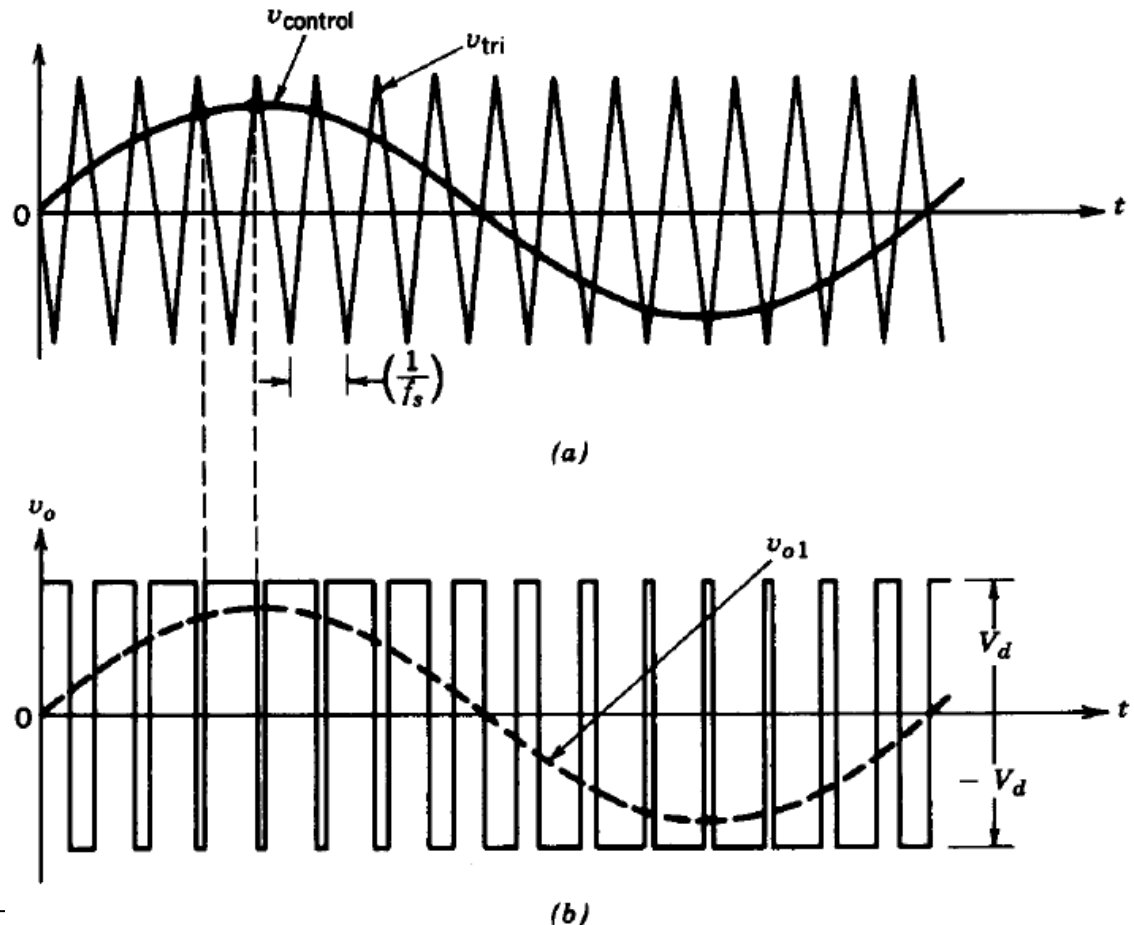


Figure 8-12 PWM with bipolar voltage switching.

# ■ Unipolar (3-level) voltage switching

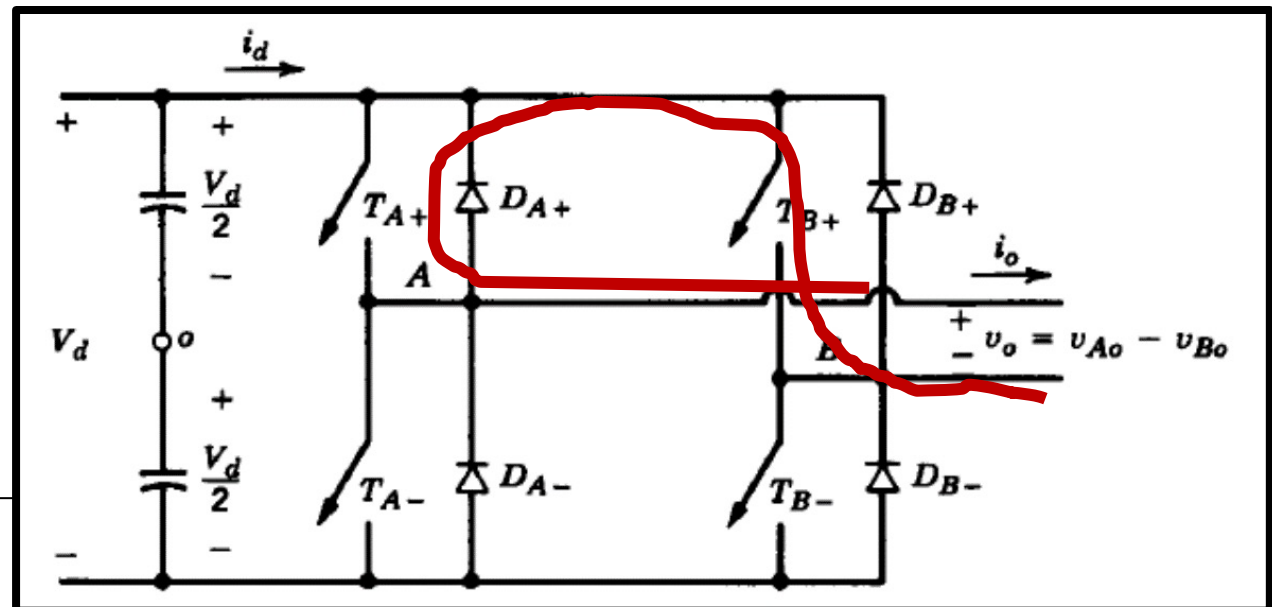
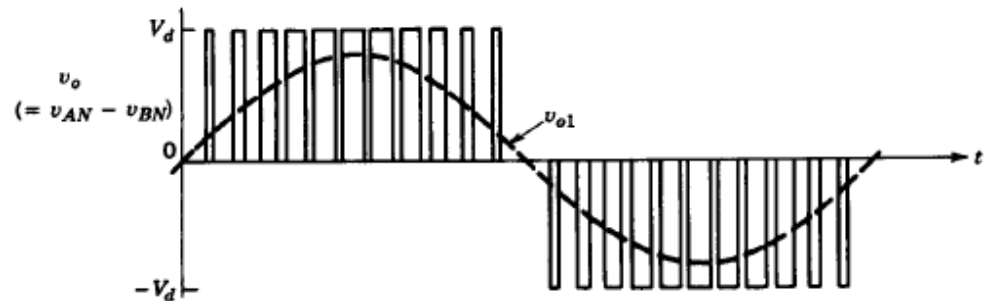
■ Switches in each inverter leg (A and B) are controlled independently of the other leg

1.  $T_{A+}$  on,  $T_{B+}$  on:  $v_o = v_A - v_B = 0$

2.  $T_{A+}$  on,  $T_{B-}$  on:  $v_o = v_A - v_B = +V_d$

3.  $T_{A-}$  on,  $T_{B-}$  on:  $v_o = v_A - v_B = 0$

4.  $T_{A-}$  on,  $T_{B+}$  on:  $v_o = v_A - v_B = -V_d$



# ■ Unipolar (3-level) voltage switching

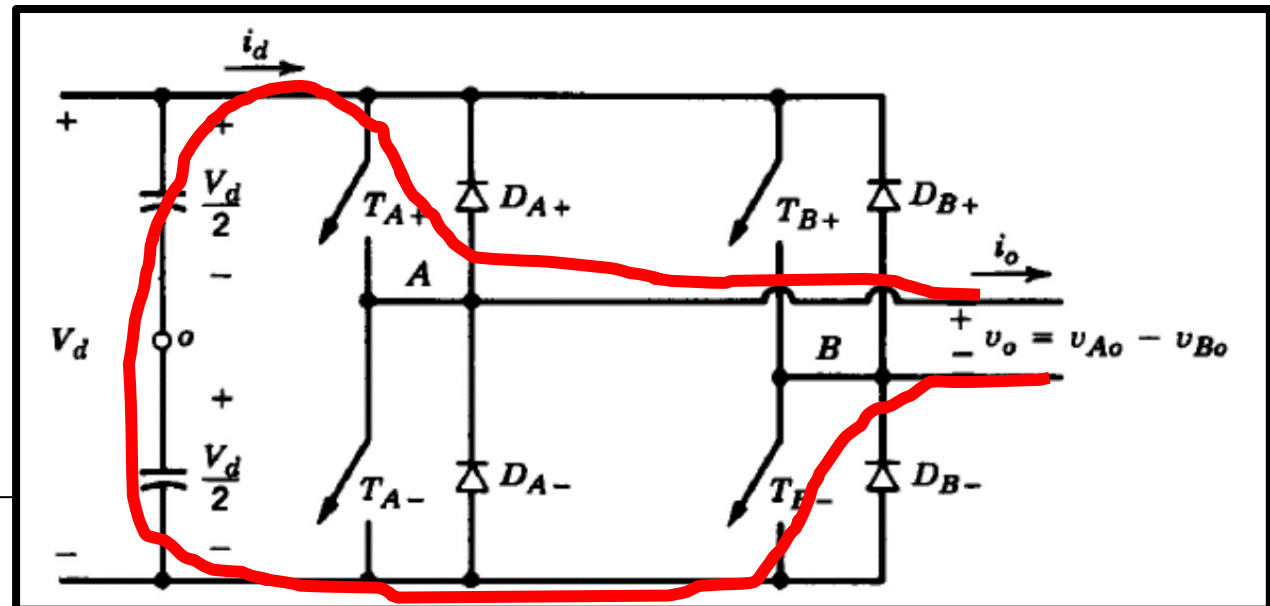
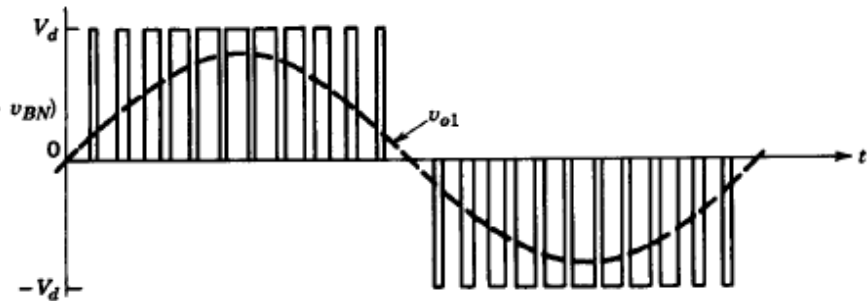
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1.  $T_{A+}$  on,  $T_{B+}$  on:  $v_o = v_A - v_B = 0$

2.  $T_{A+}$  on,  $T_{B-}$  on:  $v_o = v_A - v_B = +V_d$  ( $= v_{AN} - v_{BN}$ )

3.  $T_{A-}$  on,  $T_{B-}$  on:  $v_o = v_A - v_B = 0$

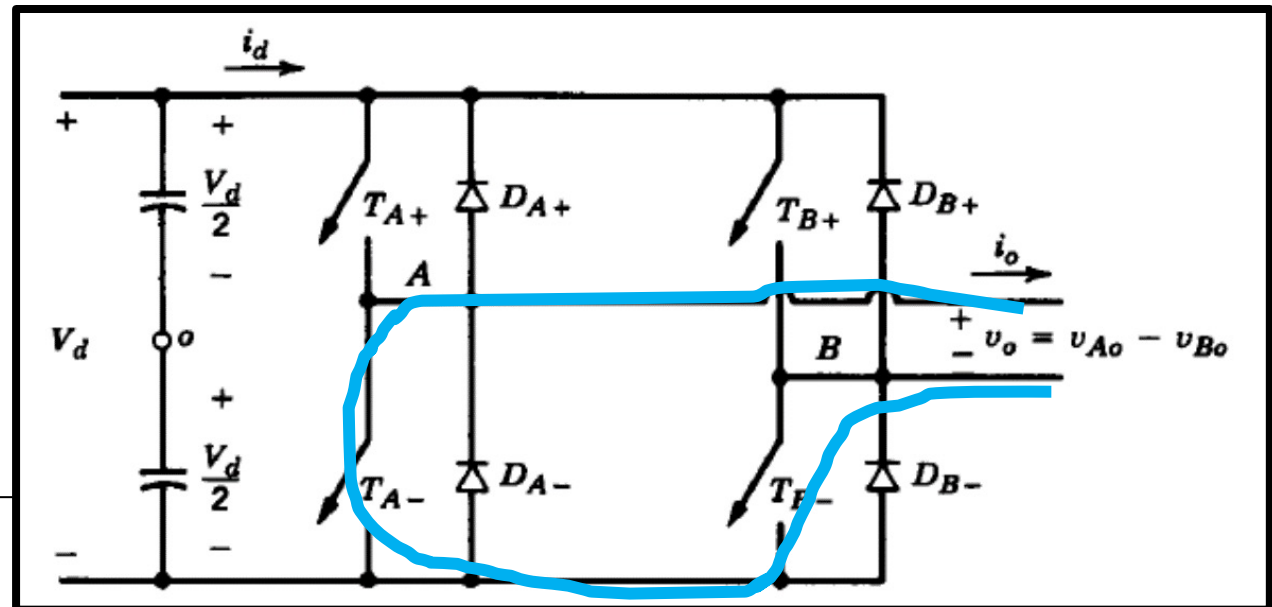
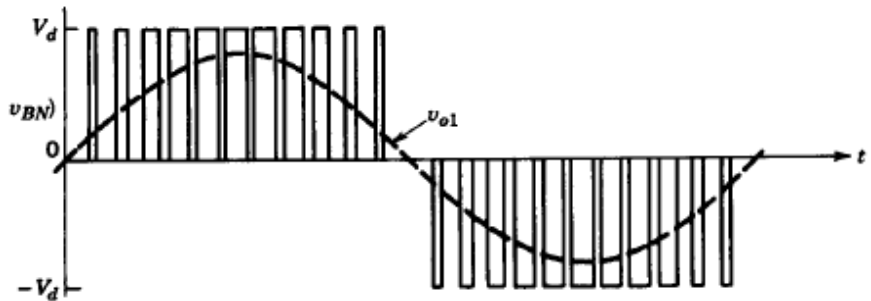
4.  $T_{A-}$  on,  $T_{B+}$  on:  $v_o = v_A - v_B = -V_d$



# ■ Unipolar (3-level) voltage switching

■ Switches in each inverter leg (A and B) are controlled independently of the other leg

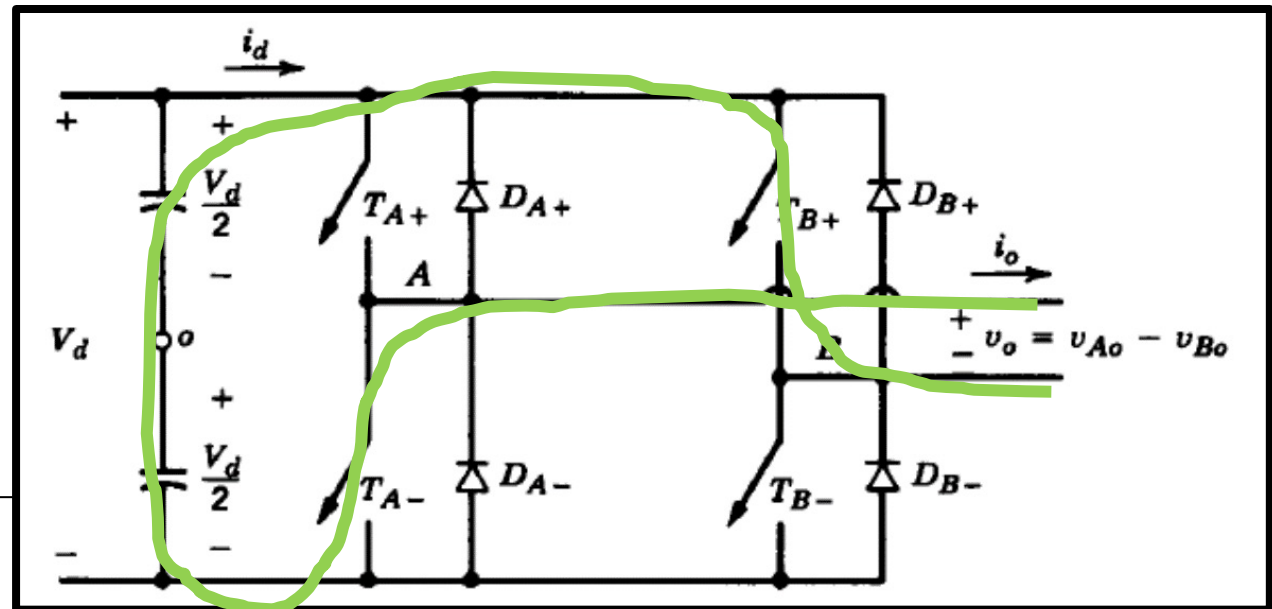
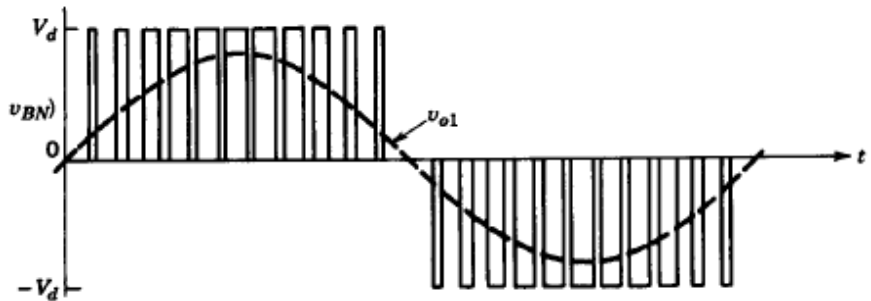
1.  $T_{A+}$  on,  $T_{B+}$  on:  $v_o = v_A - v_B = 0$
2.  $T_{A+}$  on,  $T_{B-}$  on:  $v_o = v_A - v_B = +V_d$  ( $= v_{AN} - v_{BN}$ )
3.  $T_{A-}$  on,  $T_{B-}$  on:  $v_o = v_A - v_B = 0$
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# ■ Unipolar (3-level) voltage switching

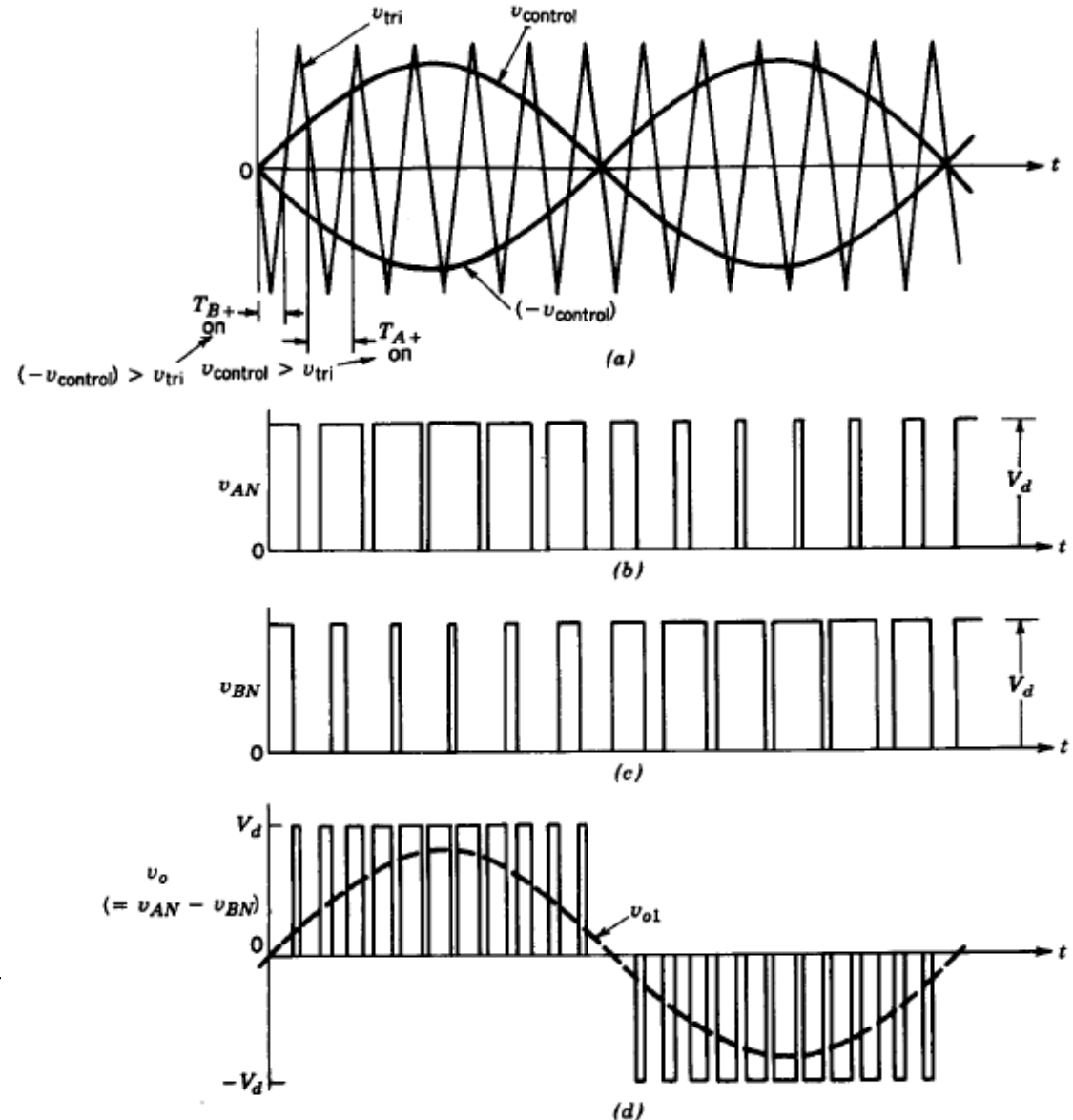
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3.  $T_{A-}$  on,  $T_{B-}$  on:  $v_o = v_A - v_B = 0$
4.  $T_{A-}$  on,  $T_{B+}$  on:  $v_o = v_A - v_B = -V_d$



# Unipolar PWM-control

- One leg controlled by  $v_{\text{control}}$
- Other leg controlled by  $-v_{\text{control}}$
- Four states
- Output voltage
  - $\hat{V}_{o1} = m_a V_d$
  - $0 < m_a < 1$



# Switch utilization ratio

- The ratio between converter power rating and the combined rating of the switches

- $$\frac{V_{o1,max} I_{o1,max}}{q V_T I_T}$$

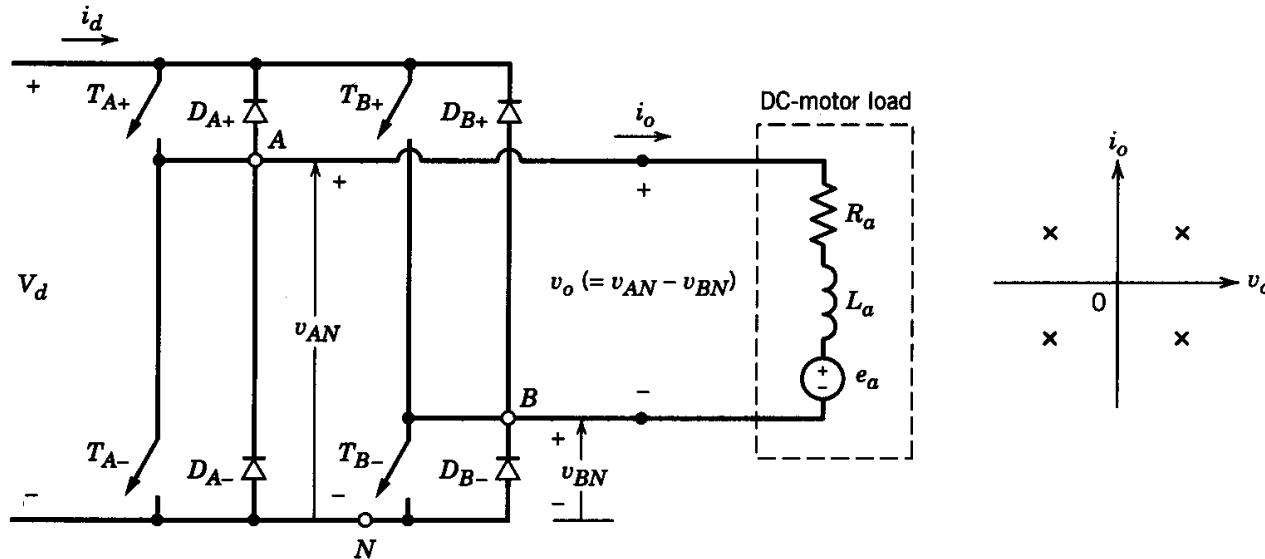
- $V_{o1,max}$  max fundamental output rms voltage
- $I_{o1,max}$  max fundamental output rms current
- $q$ : number of switches
- $V_T$ : Peak voltage rating a switching device
- $I_T$ : Peak current rating of a switching device



# Lecture 3

## Full-bridge DC/DC converter

# Full-bridge DC/DC converter



**Figure 7-27** Full-bridge dc–dc converter.

- Four quadrant operation is possible.
  - Positive or negative output voltage
  - Bidirectional current
- Common for dc-motor drives
  - Bidirectional rotation
  - Both motor and generator operation

# Converter Waveforms

- Bi-polar voltage switching

$$D_1 = \frac{t_{on}}{T_s} = \frac{1}{2} \left( 1 + \frac{v_{control}}{\hat{V}_{tri}} \right)$$

$$D_2 = 1 - D_1$$

$$V_o = V_{AN} - V_{BN} = D_1 V_d - D_2 V_d$$

$$= (2D_1 - 1)V_d$$

$$V_o = \frac{V_d}{\hat{V}_{tri}} v_{control}$$

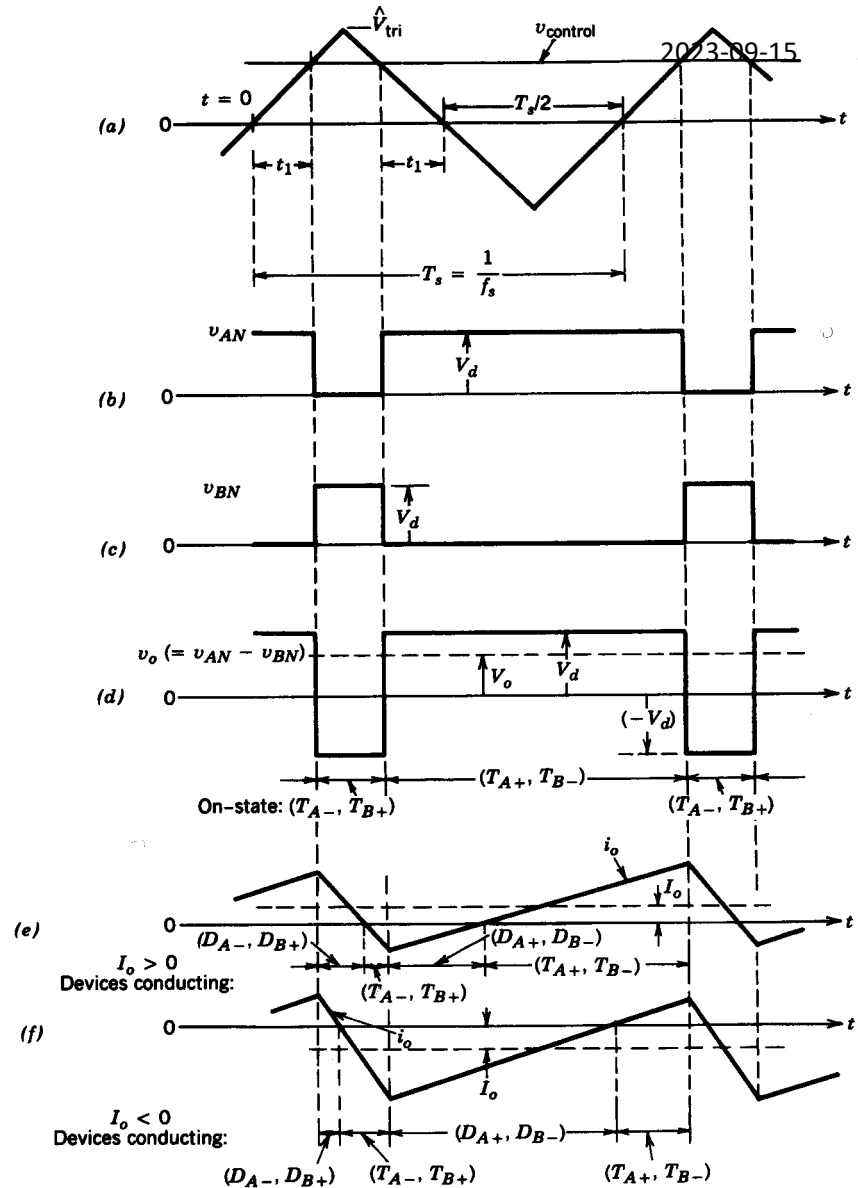


Figure 7-28 PWM with bipolar voltage switching.

# Converter Waveforms

- Uni-polar voltage switching

$$D_1 = \frac{1}{2} \left( \frac{v_{\text{control}}}{\hat{V}_{\text{tri}}} + 1 \right) \quad T_{A+}$$

$$D_2 = 1 - D_1 \quad T_{B+}$$

$$V_o = (2D_1 - 1)V_d = \frac{V_d}{\hat{V}_{\text{tri}}} v_{\text{control}}$$

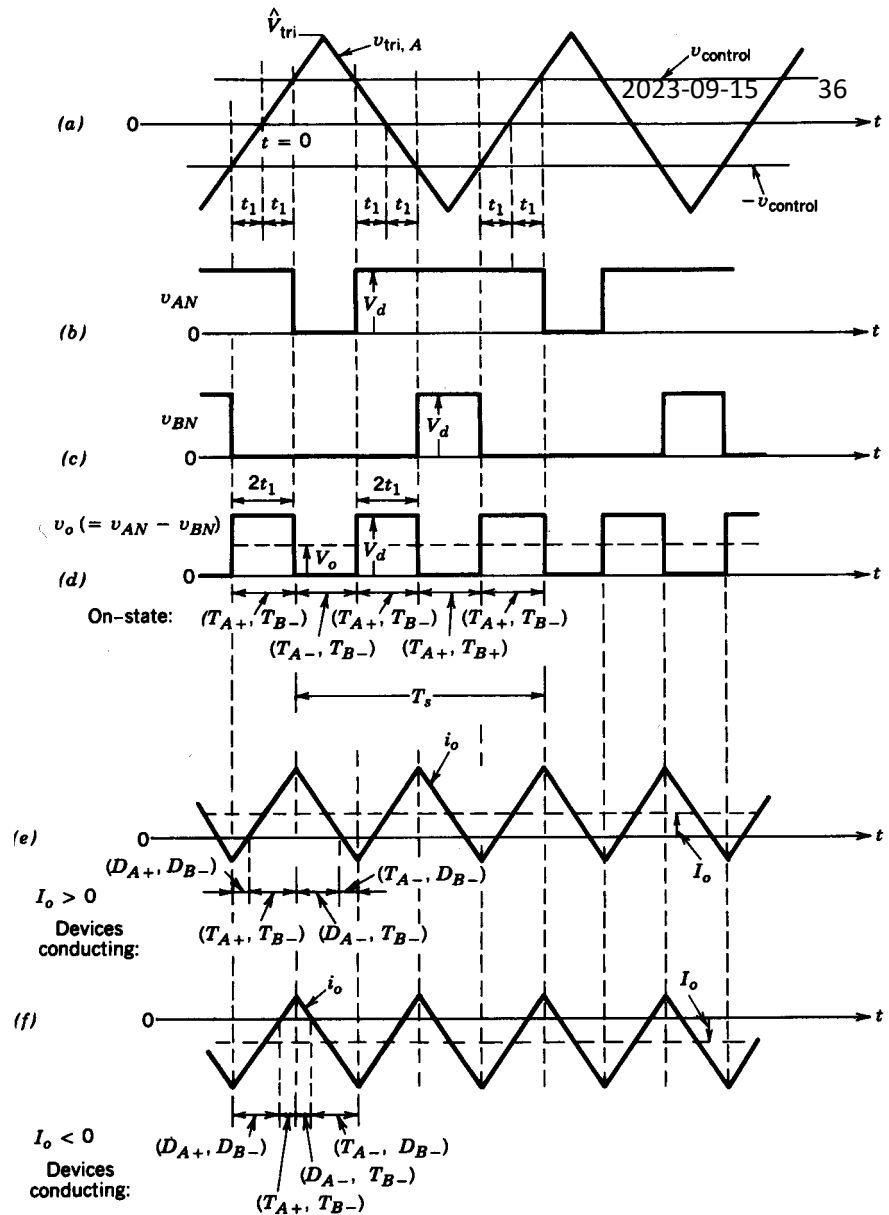


Figure 7-29 PWM with unipolar voltage switching.

Lars Eriksson

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